

## 5: Dedicated AE(AD) Schemes

- Given an IND-CPA-secure ENCR and an UF-CMA-secure MAC, Encrypt-then-MAC with ENCR and MAC guarantees secure AE.
- Though, many researchers studied homogeneous AE schemes.
- Motivation:
  - Single key (instead of two independent  $K$  and  $L$ )
  - Improved efficiency
  - Fun ;-)
- Many *dedicated* AEAD schemes in the literature
  - Similar to generic composition, with single key (CCM, GCM, EAX, ...)
  - Dedicated schemes (e.g., OCB)

# Some Issues for the design of AEAD Schemes

## ■ Efficiency:

- As fast as possible
- On a wide range of platforms (from small embedded to high-end)
- Small chip size when implemented in hardware
- Parallelism / pipelining  
(e.g., compare Counter and CBC encryption)

## ■ Security:

- Provable security
- Take care of lengths  
(e.g., when computing  $A \leftarrow \text{MAC}_K(A \parallel C)$ , an adversary might shift the boundary between associated data  $A$  and ciphertext  $C$ )

## ■ Simplicity:

- Easy to describe
- Easy to understand
- Easy to analyze
- Easy to implement correctly

## 5.1: Two-Pass Modes

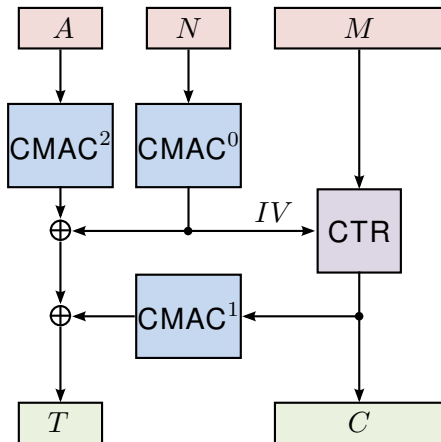
- Block-cipher-based
- “Two-pass”: one pass for encryption, one pass for authentication
- Similar to generic composition (specifically: EtM)
- Single key
- Security up to the birthday bound ( $\ll 2^{n/2}$  blocks)
- Core ideas of security proofs rather straightforward

# Notation

- Key  $K$
- Nonce  $N$
- Block cipher  $E : \{0, 1\}^k \times \{0, 1\}^n \rightarrow \{0, 1\}^n$
- Message  $M = (M_1, \dots, M_m)$
- Associated data  $A = (A_1, \dots, A_s)$
- Ciphertext  $C = (C_1, \dots, C_m)$
- Authentication tag  $T \in \{0, 1\}^n$  (most modes allow truncation)
- $|M| = |C| = n \cdot (m - 1) + |M_m|$
- $|A| = n \cdot (s - 1) + |A_s|$

# EAX

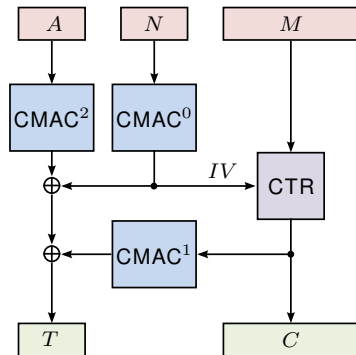
Bellare, Wagner, 2004



# EAX: Core Ideas of the Security Proof (1)

IND-CPA-Security up to the Birthday Bound

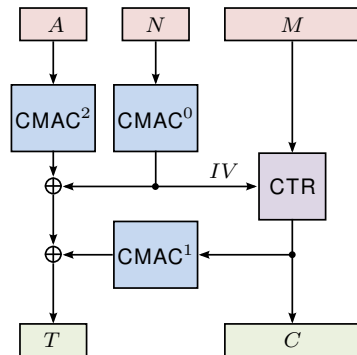
- We observe:  $\text{CMAC}^i$ -functions  $\approx$  independent random functions
- Random  $IV$  for the counter mode (for a nonce-respecting adversary!)
- $\implies$  each ciphertext is a fresh random value
- Tag: XOR of three independent random values



# EAX: Core Ideas for Security Proof (2)

## INT-CTXT-Security Up to the Birthday Bound

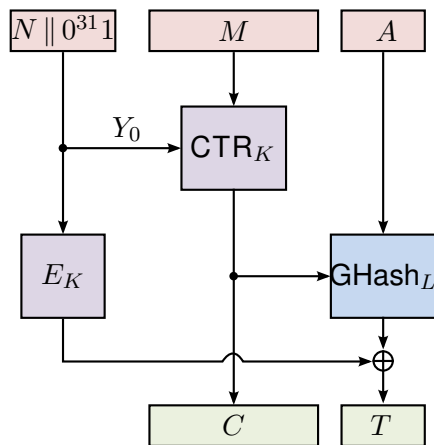
- Eve knows some tuples  $(N_i, M_i, A_i, C_i, T_i)$
- **Forgery** = valid  $(N, A, C, T)$  with  $(N, A, C, T) \notin \{(N_i, A_i, C_i, T_i)\}$
- If  $N \notin \{N_i\}$ , Eve would need to predict  $\text{CMAC}^0(N)$ , so assume  $N = N_j$  for some  $j$ .
- Similarly:  $A = A_k$  for some  $k$ , and  $C = C_\ell$  for some  $\ell$
- But not  $j = k = \ell$ , else  $(N, A, C, T) = (N_j, A_j, C_j, T_j)$ .
- $T$ : Solution of linear equation system
- But: Too few equations and too many random unknowns



# Galois Counter Mode (GCM)

McGrew, Viega, 2004

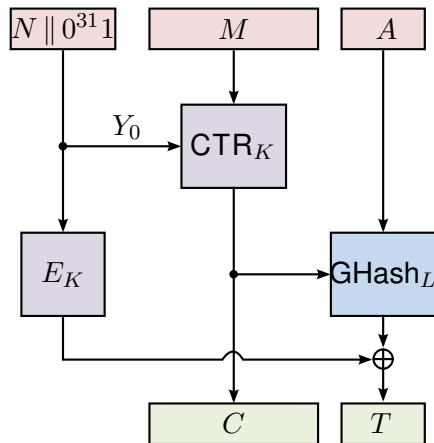
- Single key  $K$
- Derives hash key:  
 $L := E_K(0^n)$
- Polynomial Hash (GHash)
- GHash appends a length-encoding block  $|A| \parallel |M|$  for domain separation, encoded as  $n/2$ -bit values





# Properties of GCM

- If  $N$  is nonce: Inputs to  $E$  never repeat
- 96-bit nonce  $N$  and 32-bit block counter  
 $\implies |M| \leq 2^{32}$  blocks
- Since  $Y_0 \neq 0^n$ :  $E_K(0^n)$  never used again
- Carter-Wegman MAC:  
 $E_K(N \parallel 0^{31}1) \oplus$   
 $\text{GHash}_L(C, A)$



# GCM: GHash

## Definition 40 (Almost-XOR-Universal Hash Functions)

Let  $\mathcal{H} = \{H \mid H : \{0, 1\}^* \rightarrow \{0, 1\}^n\}$  be a family of hash functions.  $\mathcal{H}$  is called  $\epsilon$ -**almost-XOR-universal** ( $\epsilon$ -**AXU**) iff for  $H \xleftarrow{\$} \mathcal{H}$  and all distinct  $X, X' \in \{0, 1\}^*$  and  $\Delta \in \{0, 1\}^n$

$$\Pr [H(X) \oplus H(X') = \Delta] \leq \epsilon.$$

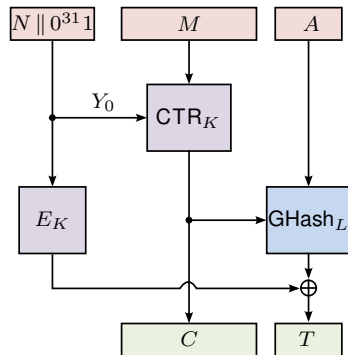
- AXU is equivalent to  $A\Delta U$  when computing in  $\text{GF}(2^n)$
- Secret key  $L \in \text{GF}(2^n)$ , fixed input length of  $m$  blocks:

$$\text{GHash}_L(X_1, \dots, X_m) = \bigoplus_{i=1}^m X_i \cdot L^i$$

- Fundamental Theorem  $\Rightarrow$  GHash is  $\epsilon$ -AXU with  $\epsilon \leq m/2^n$ .

# GCM Security (1)

- Encrypt-then-MAC with “independent” keys  $K$  and  $L$  ( $E_K(0^n)$  can never occur elsewhere)
- Iwata, Ohashi, Minematsu (2012):
  - $q$  queries of  $\sigma$  blocks in total, maximum input length  $\ell$
  - Probability to break GHash  $\leq q\ell/2^n$  ( $\rightarrow$  Thm. ??)



$$\text{Adv}_{\text{GCM}}^{\text{IND-CPA}}(q, \ell, \sigma) \leq \frac{(q + \sigma + 1)^2}{2^{n+1}}$$

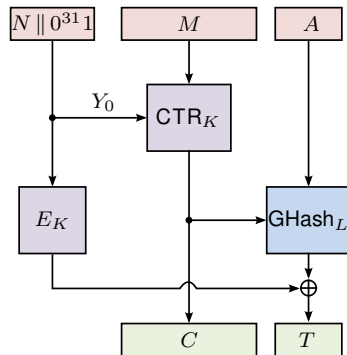
$$\text{Adv}_{\text{GCM}}^{\text{INT-CTXT}}(q, \ell, \sigma) \leq \frac{(q + \sigma + 1)^2}{2^{n+1}} + \frac{q\ell}{2^n}$$

# GCM Security (2)

- GCM also supports smaller nonces:

$$N \leftarrow \text{GHash}_L(N') \bmod 2^{96}$$

- But: Security bounds become **much worse**
- Hardly ever used in practice (fortunately)

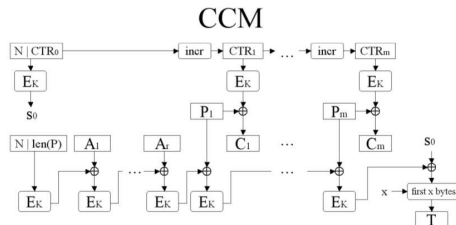


# Other Two-Pass Modes

## CCM: Counter with CBC-MAC

(Whiting, Housley, Ferguson, 2003)

- MAC-then-Encrypt
- Two-pass,  $|M|$  required early

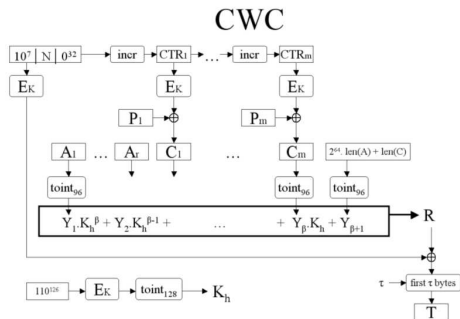


## CWC: Counter with

## Carter-Wegman

(Kohno, Viega, Whiting, 2004)

- Encrypt-then-MAC
- Two-pass
- Uses polynomial hash
- Modulo  $2^{128} - 1$



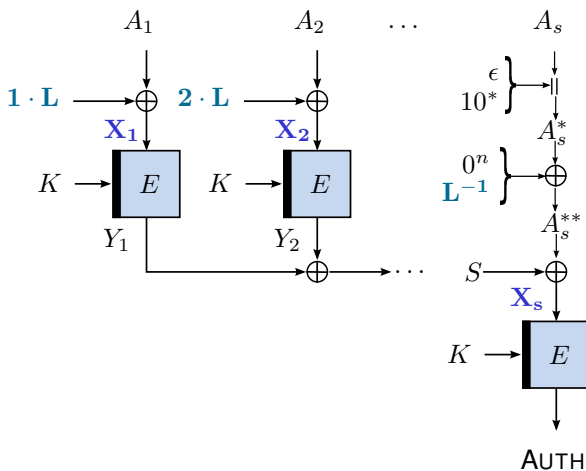
## 5.2: OCB: A Single-Pass Mode

“Offset Codebook” Rogaway et al, 2001, 2004, 2010; One-Pass

- Actually predates most two-pass modes
- Complex patent situation (three different parties claim a patent)
- A bit more complex than single-pass modes, but more efficient
- Three versions:
  - Three different ways to compute the “offsets”
  - OCB1 did not yet support associated data
  - Beyond that not many differences
  - Below: we will focus on OCB3

# OCB is the AE-sibling of PMAC

## Simplified



## OCB

Ignoring the Case of Partial  $M_m$ 

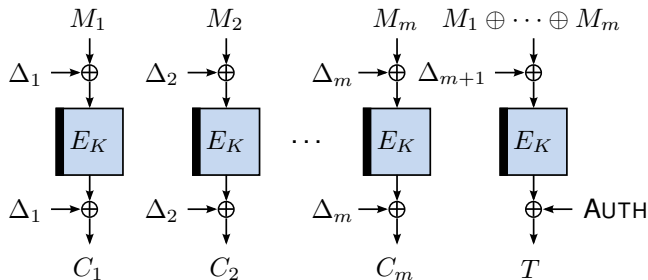
- $L \leftarrow E_K(0^n)$

- $L_0 \leftarrow 2^2 L$

- $L_i \leftarrow 2L_{i-1}$

- $\Delta_0 \leftarrow F_K(N, |T|)$

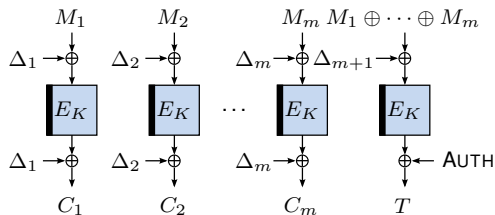
- $\Delta_i \leftarrow$   
 $\Delta_{i-1} \oplus L_{\text{ntz}(i)}$





# Remarks

- Like the two-pass modes we presented, OCB is secure up to the birthday bound.
- Security analysis is similar to that of PMAC
- The multiples of  $L$  depend only on the key
- Like PMAC,  $i \cdot L$  actually is  $g_i \cdot L$ , where  $g_i$  is a grey code
- $\Delta$  depends on the key and the nonce
- When the nonce is a counter, the computation of  $\Delta$  only needs a block-cipher call for every 64-th nonce



## 5.3: EAX-Prime

- A *minor modification* of EAX (needs slightly less storage)
- Adapted as the AE mode of operation for the proposed smart grid standard from ANSI,
- **But:** security proof is no longer applicable
- **And:** EAX' was actually broken ( $\rightarrow$  separate slides).

This is yet another shocking case of so-called “practitioners” neglecting cryptographers’ knowledge:

*I still think standards are preferable in theory, but only if they're promulgated by reasonable standards bodies. And we seem to have a shortage of those.*

*[...]*

*How can I advocate for crypto standards when standards bodies will casually throw away something as wonderful as a security proof?*

– Matthew Green

## 5.4: Discussion: Which Mode is the Best?

### ■ **OCB:**

- Very fast, almost fully parallelizable
- A bit more complex to understand and implement
- Patent situation may be an issue

### ■ **GCM:**

- Has become quite popular
- Fastest two-pass mode on most machines

### ■ **EAX:**

- May be the easiest to implement

■ In any case, take great care, if you think of creating your own!

■ At the end: All the modes presented here are OK.

■ Except for **EAX'**, of course.

■ But all these modes break apart when used improperly  
(→ next chapter)