

Animation Systems:

8. Collisions

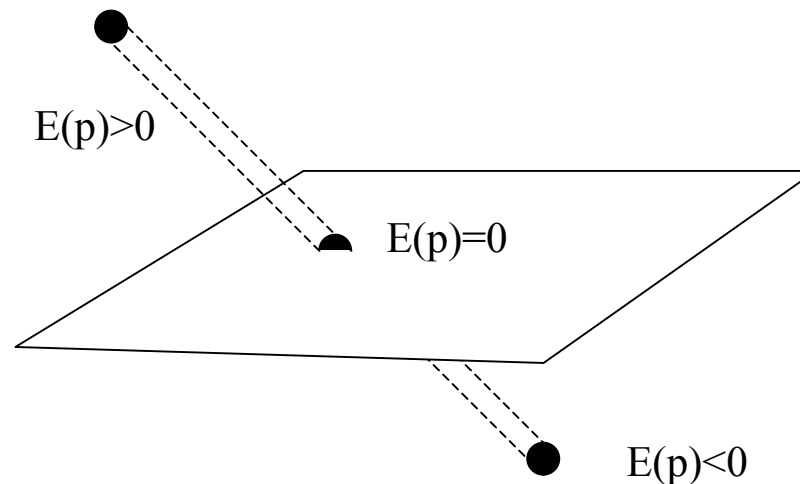
Charles A. Wüthrich
CogVis/MMC, Faculty of Media
Bauhaus-University Weimar

Collisions

- When objects start to move, they actually collide
- Two issues must be addressed:
 - Detecting collision
 - Computing appropriate response
- Detecting collision: two main approaches
 - Penalty method: calculate the reaction after collision has occurred
 - when more particles involved, assume they collided at same instant
 - Imprecise but often acceptable
- Computing the appropriate response to collision (depends on physics and distribution of mass of the object)
 - Back up time to first instant of collision and compute appropriate response
 - By heavy no of collisions, quite time consuming
 - Kinematic response
 - Penalty method: introduce a nonphysical force to restore non penetration but compute it at time of collision
 - Calculation of impulse force

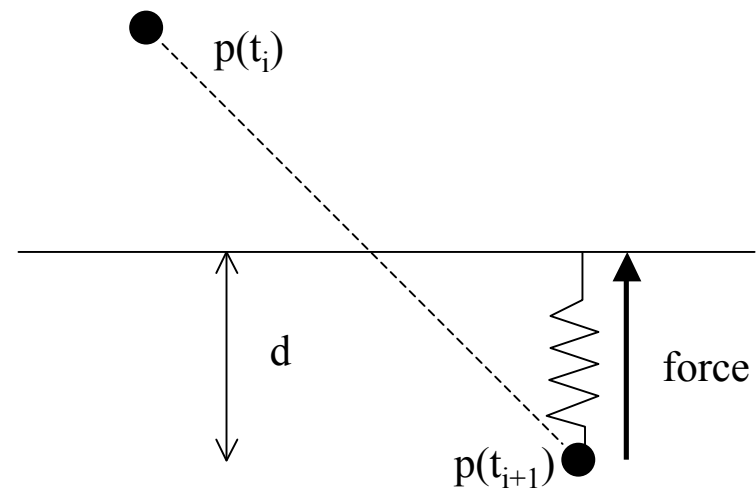
Kinematic response

- A simple case is a particle moving at constant velocity and impacting a plane
- Questions:
 - When is the impact?
 - How does it bounce off?
- Use plane equation
 $E(p): ax+by+cz+d$
- If normals correct, then
 - If $E(p)=0$ then p plane point
 - If $E(p)>0$ then p above plane
 - If $E(p)<0$ then below plane
- The particle moves with equations:
 $p(t_i)=p(t_{i-1})+t \cdot v_{ave}(t)$
- When $E(p(t_i))$ switches to ≤ 0 then we had a collision
- Now the component of the velocity parallel to the normal to the plane is negated
- Some damping factor N is added
 $v(t_{i+1})=v(t_i)-v(t_i)N-kv(t_i)N$
 $=v(t_i)-(1+k)v(t_i)N$



Penalty method

- Here we construct a reaction to the collision
- A spring with zero rest length is attached at the instant of collision
- The closest point on the surface to the penetrating point is used as attachment point
- The spring obeys Hooke's law: $F = -kd$
- The approach needs to assign arbitrary masses and constant, and therefore is not ideal
- Moreover, for fast moving points it might take a few steps to push back the obj
- For polyhedra, it might also generate torque



Polyhedras colliding

- Shape can be complicated for complex objects
- Thus, collisions can be tested before on bounding boxes
- Or by adding hierarchical bounding boxes
- Testing a point to be inside a polyhedron is not easy
- But for a polyhedron one needs to test all vertices for the two objects
- And each point has to be tested against all the planes of the faces of the polyhedron
- This works only for convex polyhedra
- For concave polyhedra, one can use a similar method to the point in polygon test
- Construct a semi-infinite ray from the point towards the polyhedron, and check no of intersections
 - If they are even, then the point is outside
 - If they are odd, then it lies inside
- Of course counting double points right has to be done
- In some cases, for solids of simple shape and moving with an easy movement, the volume of it can be swept along its trajectory

Impulse force of collision

- To do accurate computations, time has to be backed to the instant of collision
- Then the exact reaction can be computed
- If a collision appeared between t_i and t_{i+1} , then
 - recursive bisection of the time step between these two timepoints will eventually yield the exact time of the impact
 - Alternatively, a linear approximation of the velocity can be used to simplify the calculations
- At the time of the impact, the normal component of the point velocity can be modified to reflect the bounce
- This normal can be multiplied by a scalar to model the degree of elasticity of the impact
- This scalar is called coefficient of restitution

Impulse forces

- Once the simulation is backed up to the time of the collision, the reaction can be computed
- By working back from the desired change in velocity, the required change in momentum can be deduced
- This equation uses the a new term, the impulse, expressed in units of momentum
- J can be seen as a large force acting in a short time interval
- This allows computing the new momentum
- To characterize elasticity, the coeff. of restitution, ϵ is computed ($0 \leq \epsilon \leq 1$)
- The velocities along the normal before and after the impact are related by $v_{\text{rel}}^+ = -\epsilon v_{\text{rel}}^-$

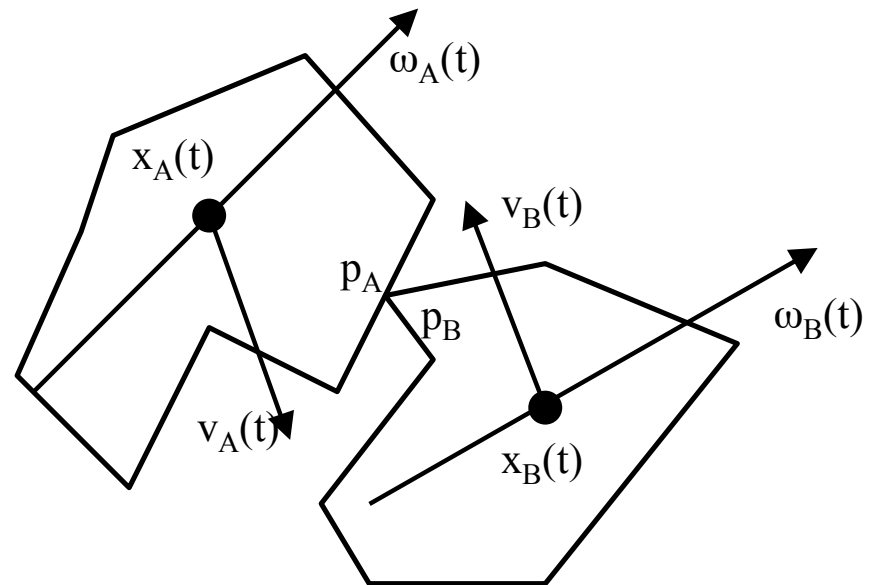
$$J = F \Delta t = M a \Delta t = M \Delta v =$$

$$\Delta(Mv) = \Delta P$$

Impulse forces

- Assume that the collisions of the two objects A and B has been detected at t
- Each obj Ob has position of mass center $x_{Ob}(t)$, lin. velocity $v_{Ob}(t)$ and ang. velocity $\omega_{Ob}(t)$
- At the point of intersection, the normal to the surface of contact is determined (note, it can be a surface, but also a point)
- Let r_A and r_B be the relative positions of the contact points WRT the center of mass
- Relative velocities of the contact points WRT center of mass and the velocities of the contact points are computed as

- $r_A = p_A - x_A(t)$
 $r_B = p_B - x_B(t)$
 $v_{rel} = (p_A^\circ(t) - p_B^\circ(t))$
 $p_A^\circ(t) = v_A(t) + \omega_A(t) \times r_A$
 $p_B^\circ(t) = v_B(t) + \omega_B(t) \times r_B$



Impulse forces

- Linear and angular velocities of the objects before the collision

$v_{ob}^- \omega_{ob}^-$ are updated $v_{ob}^+ \omega_{ob}^+$

$$v_A^+ = v_A^- + jn/M_A$$

$$v_B^+ = v_B^- + jn/M_B$$

$$\omega_A^+ = \omega_A^- + I_A^{-1}(t)(r_A \times j \cdot n)$$

$$\omega_B^+ = \omega_B^- + I_B^{-1}(t)(r_B \times j \cdot n)$$

where the impulse J is a vector quantity in the direction of the normal

$$J = j \cdot n$$

- To find the impulse, the diff between the velocities of the contact points after collision in the direction of the normal to the surface of collision is formed

$$v_{rel}^+ = n \cdot (p_A^+(t) - p_B^+(t))$$

$$v_{rel}^+ = n \cdot (v_A^+(t) + \omega_A(t) \times r_A - v_B(t) + \omega_B(t) \times r_B)$$

- Substituting previous equations one obtains

$$j = \frac{-((1 + \varepsilon) \cdot v_{rel}^+)}{\frac{1}{M_A} + \frac{1}{M_B} + n \cdot (I_A^{-1}(t)(r_A \times n)) \times r_A + (I_B^{-1}(t)(r_B \times n)) \times r_B}$$

- Contact between two objects is defined by the point on each involved and the normal to the surface of contact
- If the collision occurs, the eq. Above is used to compute the magnitude of the impulse
- The impulse is then used to scale the contact normal, and update linear and angular momenta

Friction

- An object resting on another one has a resting contact with it
 - This applies a force due to gravity which applies to both objects and can be decomposed along the directions parallel F_{Pa} to the resting surface and F_N perpendicular to it
 - The static friction force is proportional to F_N :
- Once the object is moving, there is a kinetic friction taking place. This friction creates a force, opposite to the direction of travel, and again proportional to the normal

$$F_k = \mu_k F_N$$

$$F_s = \mu_s F_N$$

Resting contact

- It is difficult to compute forces due to resting contact
- For each contact point, there is a force normal to the surface of contact
- All these forces have to be computed for all objects involved in resting contact
- For each contact point, a torque is also generated on it.
- If bodies have to rest, all those forces and torques have to be zero
- Solutions to this problem include quadratic programming, and are beyond the scope of this course

Constraints

- One problem occurring in animation is the fact that variables are not free.
- Constraints are usually set on objects and limit the field of the independent variables.
- There are two types of constraints:
 - hard constraints: strictly enforced
 - soft constraints: the system only attempts to satisfy them

Flexible objects

- Spring-mass-damper model is most used approach
- Springs: work with Hooke's law: the force applied is $F_{i,j} = -F_{j,i} = k_s(d_{i,j}(t) - \text{len}_{i,j})v_{i,j}$ where
 - d_{ij} distance between the two points
 - len_{ij} rest length of the spring
 - k_s spring constant
 - v_{ij} unit vector from point i to point j
- The flexible model is modelled as a net of points with mass and springs and dampers between them
- A damper can impart a force in the direction opposite to the velocity of the spring length and proportional to that velocity $F_i^d = -k_d v_i(t)$
- One can also introduce angular dampers and springs between faces
- Additional internal springs have often to be added to add stability to the system



Virtual springs

- Induce forces that do not directly model physical elements
- For example, in the penalty method
- Sometimes one can use a proportional derivative controller which controls that a certain variable and speed is close to the desired value
- For example, this is used to keep the object close to the desired speed
- A virtual spring is added to keep things as desired

Energy minimization

- One can use energy to control the motion of the objects
- Energy constraints can be used to pin objects together, to restore the shape of an object, to minimize the curvature of a path or trajectory
- Energy constraints induce restoring forces on the system

Controlling groups of objects

- A *particle system* is a large collection of individual elements which taken together represent a conglomerate object
- The „global“ behaviour of the particles is called *emergent behaviour*
- This can be used both for particle systems (which usually have more individuals) and for *flocking*
- Flock members have a more sophisticated behaviour than a simple element of particle system
- While particle systems behave according to physics, flocking particles add some intelligence to the behaviour of the individuals
- The more intelligence is added, the more the element moves in a more interesting way, and the more it shows *autonomous behaviour*

Particle systems

- In a particle system, due to the no of its elements, simplified assumptions are made
- Typical assumptions are
 - Particles do not collide among themselves
 - Particles do not cast indiv. shadows, but the aggregate may do
 - Particles only cast shadows on the rest of the environment, not among themselves
 - Particles do not reflect light, each is modeled as a point light source
- Often particles are modeled as having a finite life span
- To avoid dull behaviour, often randomness is added
- When a particle system is computed, the following steps are taken:
 - Generate new particles born this frame
 - Initialize attributes of new particle
 - Remove dying particles
 - Animate active particles
 - Render them

Particle generation

- Particles are usually generated according to a stochastic process
 - At each frame, a random number r_p of particles is generated
 - Generation has a user specified distribution centered at the desired number of particles per frame
 - $r_p = \text{ave} + \text{Rand}(\text{seed}) \cdot \text{range}$ where ave is the desired average and range is the desired variation range
- Sometimes it may be convenient to have this random function as a function of time, i.e. to make the number of desired particles increase in time
- If the particles are used to model a fuzzy object, then the area of the screen covered by the object A_s is used to control the number of particles
$$r_p = \text{ave} + \text{Rand}(\text{seed}) \cdot \text{range} \cdot A_s$$

Particle attributes

- Attributes of the particles are typically
 - Position
 - Velocity
 - Shape parameters
 - Color
 - Transparency
 - Lifetime
- At each frame, the lifetime of each particle is decremented by one until it reaches zero
- During lifetime, particles are animated (position, velocity, shape, color, transparency)
- At each frame, forces on the particles are computed
- These result in an acceleration, which determines a velocity
- Also other attributes may be a function of time
- Rendering is often done modeling them as a point light source adding color to the pixel
- This to avoid particles to contribute to lighting computations

Flocks

- Here the number of members is small
- But each member has some intelligence and simple physics (avoid collision, gravity, drag)
- Aggregate behavior emerges from the members (emergent behavior)
- Each member is called a boid
- Two forces govern flock behavior:
 - collision avoidance: both with other boids and with obstacles
 - Motion has some random parameter to keep it from looking regular
 - flock centering: the boid tries to be a flock member
 - Flock centering keeps together the flock but does not have to be absolute, otherwise flocks cannot split around objects

Flocks: local behavior

- Controlling locally the behavior is the aim
- Three processes may be modeled:
 - Physics: similar to particle with gravity, collision detection and response
 - Perception of the environment: each boid views its direct neighbors and obstacles directly in front
 - Reasoning and reaction to determine the behavior
 - Additionally velocity matching is added (each boid tries to match the speed of its neighbours)
- Global control is either applied to all boids or to a group leader
 - In this case the boids follow the leader
- The leader role can be rotated among boids in time
- Usually all this is implemented as three controllers which are prioritized in the following order: collision avoidance, velocity matching and flock centering

Flock complexity

- The major problem with flocks is the fact that processing complexity is n^2 .
- Even if interactions are allowed only with k nearest neighbors, those have to be found
- One way to find efficiently is to perform a 3d bucket sort and then check adjacent buckets for neighbors
- Of course, efficiency depends on the bucket size:
 - The more buckets, the less boids per bucket
- Another way of doing it is through message passing, where each boid informs the flock of its whereabouts

Collision avoidance

- There are several ways to avoid collisions
 - The simplest way is adding a repelling force around an object
 - However, this looks weird as the boid keeps attempting to aim at the repelling surface and constantly gets blown away
 - Another method computes if the boid trajectory hits the surface and starts a steering behavior
 - Quite complicated is the simulation of a splitting flock around an obstacle, since a balance has to be found between collision avoidance and flock cohesion

Autonomous behaviour

- Modeling intelligent behaviour is a complex task
- Autonomous behaviour models an object knowing about its environment
- This can become as complicated as one wants
- Usually applied to animals, but also to people, cars on a road, planes, or soldiers in a battle
- Knowledge of the environment is provided by providing access to the environment geometry
- Subjective vision can be achieved by rendering the environment from the point of view of the object
- Internal state is modeled by intentions = the urge to satisfy a need
- High level goals can be decomposed in single low level tasks (levels of behaviour)
- Internal state and knowledge of the environment are input to the reasoning unit, which produces a strategy (=what needs to be done)
- Such strategy is turned into a sequence of actions by the planner, and actions are turned into movement
- If intentions are competing, they must be prioritized

End



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