

6. Functions and Libraries

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Introduction

- When writing programs, until now we have written our code as a part of the main program.
- To organize the programs better, it makes sense to subdivide the tasks into smaller self contained chunks, i.e. functions or, in Java, *static methods*
- For example, you might want
 - your main program to deal with user input,
 - While the actual drawing is done in a separate part

Functions (distance)

```
// ClicksDistance: Computes distance between two points
// usage: java Distance x1 y1 x2 y2

public class Distance {
    public static void main(String[] args) {
        double x1=0.0,y1=0.0,x2=0.0,y2=0.0;
        double distan;

        x1=Double.parseDouble(args[0]);
        y1=Double.parseDouble(args[1]);
        x2=Double.parseDouble(args[2]);
        y2=Double.parseDouble(args[3]);

        distan=Math.sqrt((x2-x1)*(x2-x1)+(y2-y1)*(y2-y1));
        System.out.println(distan);
    } // main
} // Distance
```

Functions (distance)

- To make it a bit simpler, I can separate the **calculation** from the input and output processing

```
// ClicksDistance: Computes distance between two points  
// usage: java Distance x1 y1 x2 y2
```

```
public class Distance {  
    public static void main(String[] args) {  
        double x1=0.0,y1=0.0,x2=0.0,y2=0.0;  
        double distan;  
  
        x1=Double.parseDouble(args[0]);  
        y1=Double.parseDouble(args[1]);  
        x2=Double.parseDouble(args[2]);  
        y2=Double.parseDouble(args[3]);  
  
        distan=Math.sqrt((x2-x1)*(x2-x1)+(y2-y1)*(y2-y1));  
        System.out.println(distan);  
    } // main  
} // Distance
```



Make this
a method

Functions (distance)

```
// ClicksDistanceFun: Computes distance between two points  
// usage: java Distance x1 y1 x2 y2
```

```
public class DistanceFun {  
    public static double distance(double x1, double y1, double x2, double y2){  
        double distance,xdiff,ydiff;  
  
        xdiff=x2-x1;  
        ydiff=y2-y1;  
        distance=xdiff*xdiff+ydiff*ydiff;  
        distance=Math.sqrt(distance);  
        return distance;  
    }  
}
```

Static method

```
public static void main(String[] args) {  
    double x1=0.0,y1=0.0,x2=0.0,y2=0.0;  
    double distan;  
  
    x1=Double.parseDouble(args[0]);  
    y1=Double.parseDouble(args[1]);  
    x2=Double.parseDouble(args[2]);  
    y2=Double.parseDouble(args[3]);  
  
    distan=distance(x1,y1,x2,y2);  
    System.out.println(distan);  
} // main  
} // DistanceFun
```

Functions (distance)

```
// ClicksDistanceFun: Computes distance between two points  
// usage: java Distance x1 y1 x2 y2
```

```
public class DistanceFun {  
    public static double distance(double x1, double y1, double x2, double y2){  
        double distance,xdiff,ydiff;  
  
        xdiff=x2-x1;  
        ydiff=y2-y1;  
        distance=xdiff*xdiff+ydiff*ydiff;  
        distance=Math.sqrt(distance);  
        return distance;  
    }  
}
```

Definition

Arguments

Return value

```
public static void main(String[] args) {  
    double x1=0.0,y1=0.0,x2=0.0,y2=0.0;  
    double distan;  
  
    x1=Double.parseDouble(args[0]);  
    y1=Double.parseDouble(args[1]);  
    x2=Double.parseDouble(args[2]);  
    y2=Double.parseDouble(args[3]);  
  
    distan=distance(x1,y1,x2,y2);  
    System.out.println(distan);  
} // main  
} // DistanceFun
```

Method call

Functions (distance)

- When the `main` is executed, when the program encounters the function call it executes the code in the function.
- It passes to the function the values of the parameters
- The static function receives these values, processes its instructions, and when it ends, it passes back to the calling program the variable following the keyword `return`
- So

```
return distance;
```

means:
 - When you go back to the calling program, in this case `main`, give back the content of the variable `distance` to the calling program

Functions (distance)

```
// ClicksDistanceFun: Computes distance between two points  
// usage: java Distance x1 y1 x2 y2
```

```
public class DistanceFun {  
    public static double distance(double x1, double y1, double x2, double y2){  
        double distance,xdiff,ydiff;  
  
        xdiff=x2-x1;  
        ydiff=y2-y1;  
        distance=xdiff*xdiff+ydiff*ydiff;  
        distance=Math.sqrt(distance);  
        return distance; }  
}
```


Signature

 Return value, must be same
type as in signature

```
public static void main(String[] args) {  
    double x1=0.0,y1=0.0,x2=0.0,y2=0.0;  
    double distan;  
  
    x1=Double.parseDouble(args[0]);  
    y1=Double.parseDouble(args[1]);  
    x2=Double.parseDouble(args[2]);  
    y2=Double.parseDouble(args[3]);  
  
    distan=distance(x1,y1,x2,y2);  
    System.out.println(distan);  
} // main  
} // DistanceFun
```

 Method call, same variable
types as in signature

Functions (distance)

- Properties of static methods:
 - Multiple arguments (you can pass as many as you want)
 - Multiple methods (a Java program can have as many methods as necessary)
 - Overloading: methods with different signatures are considered different methods
 - Multiple returns: you can put as many return statements as you like: the method will return to the calling method when it reaches the first one it encounters
 - Single return values: a method gives to the calling program a single value (but also `void` is allowed, i.e. no return values)

Functions (distance)

- Scope of a variable
 - Is the part of a program that can refer to a certain variable by name.
 - When a static method declares a variable, it can be only referred to in that block, and not elsewhere in the program.
 - So new variables in a method live only inside that method.

```
// ClicksDistanceFun: Computes distance between two points
// usage: java Distance x1 y1 x2 y2

public class DistanceFun {
    public static double distance(double x1, double y1,
                                  double x2, double y2){
        double distance,xdiff,ydiff; ← Cannot be reached
                                        from main

        xdiff=x2-x1;
        ydiff=y2-y1;
        distance=xdiff*xdiff+ydiff*ydiff;
        distance=Math.sqrt(distance);
        return distance;
    }
}

public static void main(String[] args) {
    double x1=0.0,y1=0.0,x2=0.0,y2=0.0;
    double distan;

    x1=Double.parseDouble(args[0]);
    y1=Double.parseDouble(args[1]);
    x2=Double.parseDouble(args[2]);
    y2=Double.parseDouble(args[3]);

    distan=distance(x1,y1,x2,y2);
    System.out.println(distan);
} // main
} // DistanceFun
```

Functions (distance)

- **Notice!** When passing the arguments the function makes for its scope COPIES of the arguments: modifications will not be seen by the calling function
- This is called *call by value*
- However, if you pass an array as an argument then the modifications to it will be seen by the caller
 - Reason for this: when an array is passed, only the reference to where it is in memory is passed, but no elements are copied.

```
// swaps array elements i and j
public static void exchange(String[] a, int i, int j) {
    String temp = a[i];
    a[i] = a[j];
    a[j] = temp;
}
- }
```

Functions (distance)

- Now that we know functions, we can as well use it for our two points program
- We capture the mouse position for 2 clicks, and compute the distance of the points we clicked
- We can do this by using the same DistanceFun we used in the simple program, and copying it at top of the two points program

Functions (distance)

- Now that we know functions, we can as well use it for our two points program
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Function example

- Now that we know a distance functions, we can use it for example, to write a program that
 - opens a window
 - waits for two mouse clicks
 - computes the distance between the clicked points
- We will base the example on the Mouseclick function seen in the last lecture
- However, this time we need two points for computing the distance, and to wait for the user to give 2 points
- Waiting for two points is quite tricky:
 - Remember if you clicked a first one
 - Draw line when you have two (so remember if you clicked a second)

Function example

- We can start here:

```
// mouseClicked: Draws a circle at mouse position
// usage: java mouseClicked

public class mouseClicked {
    public static void main(String[] args) {
        double x1,y1;
        boolean ispressed=false;
        double radius; // radius of circle

        StdDraw.setPenColor(255,0,0);
        radius=0.01;

        while (true) {
            ispressed=StdDraw.mousePressed();
            if(ispressed){
                x1=StdDraw.mouseX();
                y1=StdDraw.mouseY();
                StdDraw.filledCircle(x, y, radius);
                ispressed=false;
            }
        }
    } // main
} // mouseClicked
```

Click two points

```
// ClicksLine: Draws line between two points
// usage: java ClicksLine
public class ClicksLine {
    public static void main(String[] args) {
        double x1=0.0,y1=0.0,x2=-1.0,y2=-1.0;
        double mousex=-2.0, mousey=-2.0;
        boolean ispressed=false;
        boolean plfilled=false;
        double radius;    // radius of circle

        StdDraw.setPenColor(255,0,0);
        radius=0.01;

        while (true) {
            ispressed=StdDraw.mousePressed();
            if(ispressed){
                while(true){
                    // check when the user releases the mouse
                    ispressed=StdDraw.mousePressed();
                    if(!ispressed) break;
                }
                // at this point the user released the mouse:
                // now fetch its coordinates
                mousex=StdDraw.mouseX();
                mousey=StdDraw.mouseY();
            }
        }
    }
}
```

- Notice the code at the bottom:
 - while(true) means FOREVER
 - There are two of them
 - First one is the main loop for the window drawn
 - Second one does nothing until the mouse button is released
 - When it is released, it reads the coordinates of the mouse
 - So when I finish this part I have the x and y of the mouse

Click two points

```
// have we already filled the first point?  
if(p1filled == false){  
    // then copy the mouse coordinates to it  
    x1=mousex;  
    y1=mousey;  
    // draw a circle at this point  
    StdDraw.filledCircle(x1, y1, radius);  
    System.out.println("X1: " + x1 + ", " + y1);  
    // now remember that the first point was filled  
    p1filled=true;  
}
```

- Now I have my mouse:
to draw a line I need 2 points
Notice the IF at the start?
 - P1filled is a boolean control variable:
true if I already have 1pt
false if not
 - If I don't have 1st pt
we copy the captured mouse position to x1 and y1
 - AND we set P1filled to true, so next time we don't fill again 1st point

Click two points

```
else{
    // if we are here, the first point was filled:
    // so mousex and mouse y have the coordinates
    // of the second point
    x2=mousex;
    y2=mousey;
    // Draw second point
    StdDraw.filledCircle(x2, y2, radius);
    System.out.println("X2:" + x2 + ", " + y2);
    // Draw Line joining the points
    StdDraw.setPenColor(0,0,255);
    StdDraw.line(x1,y1,x2,y2);
    StdDraw.setPenColor(255,0,0);

    // now we have drawn, so reset control variable
    p1filled=false;
    // reset also mouse press control ispressed
    ispressed=false;
} // else

} // if ispressed
// StdDraw.pause(10);
} // while
} // main
} // ClicksLine
```

- The else is for filling the 2nd point and draw
- Now we know 1st point is filled
- If we are here, we have the mouse coords. For the 2nd point
- Draw the circle at the point
- We have both points, so we draw a line between them
- Finally, we clear two control variables:
 - p1filled for p1
 - ispressed for mouse press

Click two points

- Why did we use the mouse position when the mouse is released and not when the mouse is pressed?
- Because a user presses the mouse slowly compared to the speed of your computer
- So you get too many pressed mouse events which makes it difficult to control what is being filled where
- The user releases the mouse only once!

Click two points (distance)

- And the distance of the two points?
- Easy! Remember the distance function we did b4?

```
// ClicksDistanceFun: Computes distance between two points
// usage: java Distance x1 y1 x2 y2

public class DistanceFun {
    public static double distance(double x1, double y1,
                                  double x2, double y2){
        double distance,xdiff,ydiff;

        xdiff=x2-x1;
        ydiff=y2-y1;
        distance=xdiff*xdiff+ydiff*ydiff;
        distance=Math.sqrt(distance);
        return distance;
    }
}
```

- We simply add (copy) it after the
public class clickline{
line at the top

```
// compute and print the length
length=distance(x1,y1,x2,y2);
System.out.println("length: "+ length);
```

- And use it for computing (and then printing) the distance after having drawn the line

Reusing code

- For the distance calculations, we did not have to write ANY new code!
- We can REUSE what we did before!
- So, if when you develop your code, try to make it *modular*:
 - Reusable chunks
 - Encapsulated functions you can reuse when you write other code

Using static methods elsewhere

- For referring to a static method of one class in another class
- You must make both classes accessible to Java
 - Simplest way: putting them in the same directory
- Then you can refer the function as
`classname.functionname`
the dot says the function is a method of classname
- For example, in our program we can avoid to paste the distance function in our code and write:
`length=DistanceFun.distance(x1, y1, x2, y2);`
- Which is EVEN BETTER!

Libraries

- Code designed to reuse in other programs is called a *library*
- Some terminology must be introduced:
 - Clients: a client is a program using a library
 - API (Application Programming Interface): a description of the methods available in a library with their usage detail for example, the signatures of the functions
 - Implementation: the java code implementing the methods of a specific API
 - Example: implement the following API

```
public class Matrix
```

<code>double dot(double[] a, double[] b)</code>	<i>vector dot product</i>
<code>double[][] multiply(double[][] a, double[][] b)</code>	<i>matrix-matrix product</i>
<code>double[][] transpose(double[][] a)</code>	<i>transpose</i>
<code>double[] multiply(double[][] a, double[] x)</code>	<i>matrix-vector product</i>
<code>double[] multiply(double[] x, double[][] a)</code>	<i>vector-matrix product</i>

Recursion

- Now that we know more about functions, we can introduce an elegant concept called *recursion* that is often used in programming.
- In recursion, a method calls itself.
- This in Java is perfectly legitimate, and can be used to perform special computations, for example for simplifying computations until the computation is simple.
- When using recursion, one must make sure that the recursive call of the function ends at some point
 - otherwise the program makes an infinite loop, calling itself forever and ever.

Recursion: Example

- Perhaps the easiest example of recursion is given by computing the factorial of a number
 - The factorial of a number N , indicated as $N!$, is defined as the multiplication of all numbers smaller or equal to N
$$N! = N * (N-1) * (N-2) * \dots * 2 * 1$$
- There are two ways of computing the factorial of a number:
 - Through a loop
 - Through recursion, which is particularly elegant
- We can observe that
 - $N! = N * (N-1)!$
 - $(N-1)! = (N-1) * (N-2)!$
 - ...
 - $1! = 1$

Recursion: Example

- So... to compute the factorial of a number N one must
 - Multiply N with the factorial of N-1 until we reach 1

```
public static long factorial(long n) {  
    if (n == 1) return 1;  
    return n * factorial(n-1);  
}
```

- Simple and elegant!
- Nota Bene: the first line absolutely important!
 - If not there, the recursion continues FOREVER!

Recursion: Example

- Now the whole class computing our factorial allowing us to test:

```
public class Factorial{
    public static long factorial(long n) {
        if (n == 1) return 1;
        return n * factorial(n-1);
    } // factorial

    public static void main(String[] args) {
        long f;
        f=Long.parseLong(args[0]);
        f=factorial(f);
        StdOut.println("factorial="+f);
    } // main
} // Factorial
```

- Executing:
> java Factorial 6
720

Factorial: Overflow

- Factorials become very quickly huge numbers!
 - Executing:

```
> java Factorial 20
factorial=2432902008176640000
```
 - But:

```
> java Factorial 21
factorial=-4249290049419214848
```
 - This is impossible!
Cannot be a negative number!
- What happened is called *variable overflow*:
multiplying $21 * 2432902008176640000$ is a number which is too big for a double variable!
- The result of the multiplication is garbage!

Recursion: a 2nd example

- Let's get away from numbers, and do recursive visuals

Recursion: a 2nd example

```
public class RecursiveSquares {  
  
    // plot a square, centered on (x, y) of the given side length  
    // with a light gray background and black border  
    public static void drawSquare(double x, double y, double size) {  
        StdDraw.setPenColor(StdDraw.LIGHT_GRAY);  
        StdDraw.filledSquare(x, y, size/2);  
        StdDraw.setPenColor(StdDraw.BLACK);  
        StdDraw.square(x, y, size/2);  
    }  
  
    // plot an order n recursive squares pattern  
    // centered on (x, y) of the given side length  
    public static void draw(int n, double x, double y, double size)  
    {  
        if (n == 0) return;  
  
        drawSquare(x, y, size);  
  
        // 2.2 ratio looks good  
        double ratio = 2.2;  
  
        // recursively draw 4 smaller trees of order n-1  
        draw(n-1, x - size/2, y - size/2, size/ratio); // lower left  
        draw(n-1, x - size/2, y + size/2, size/ratio); // upper left  
        draw(n-1, x + size/2, y - size/2, size/ratio); // lower right  
        draw(n-1, x + size/2, y + size/2, size/ratio); // upper right  
    }  
}
```

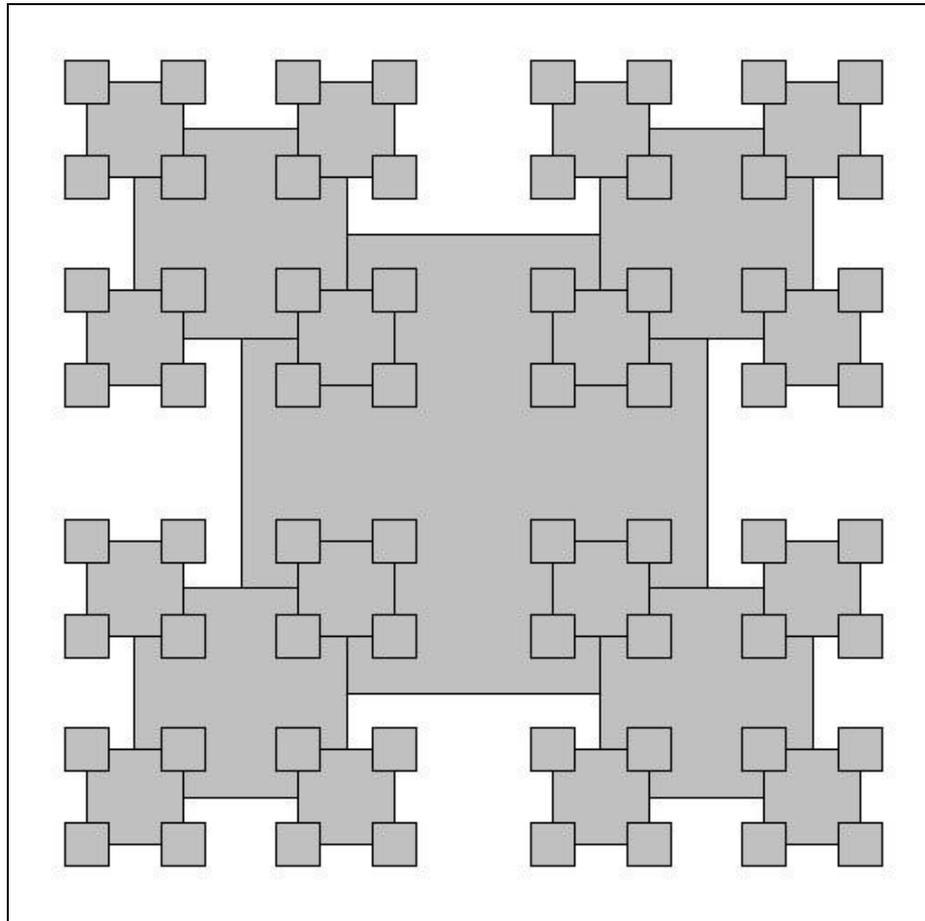
Recursion: a 2nd example

```
// read in an integer command-line argument n and plot
// an order n recursive squares pattern
public static void main(String[] args) {
    int n = Integer.parseInt(args[0]);

    double x = 0.5, y = 0.5; // center of square
    double size = 0.5; // side length of square
    draw(n, x, y, size);
}
}
```

Recursion: a 2nd example

- Resulting execution (4 recursions)



End

+++ Ende - The end - Finis - Fin - Fine +++ Ende - The end - Finis - Fin - Fine +++