

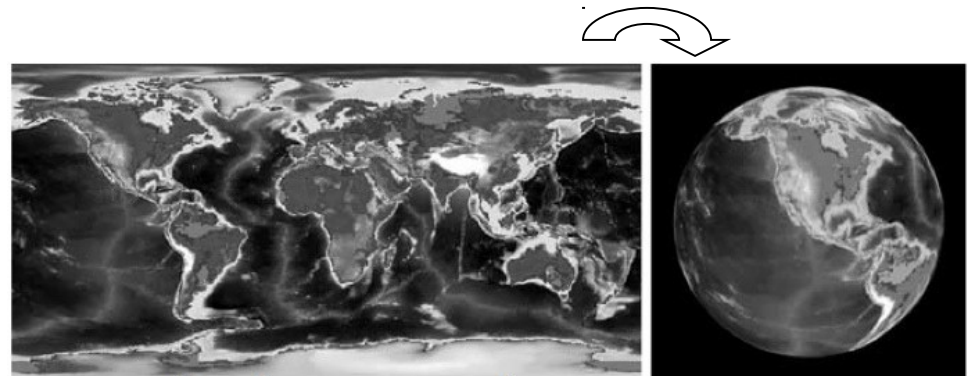
Computer Graphics:

4-Textures and shadows

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Textures

- We have been looking at light reflectance for surfaces which have no detail on the surface
- In fact, reality shows richness of surface detail.
- One could model the surface with detailed geometry
- However, this would increase greatly the complexity of the model.
- A better approach is therefore to „paint“ detail on simple geometry
- The image, called texture, is „glued“ to a simple geometry to obtain detail
- First approaches due to Catmull (74) and Blinn & Newell (76)



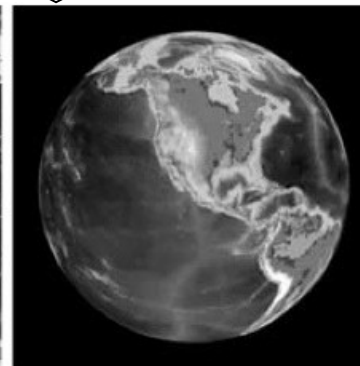
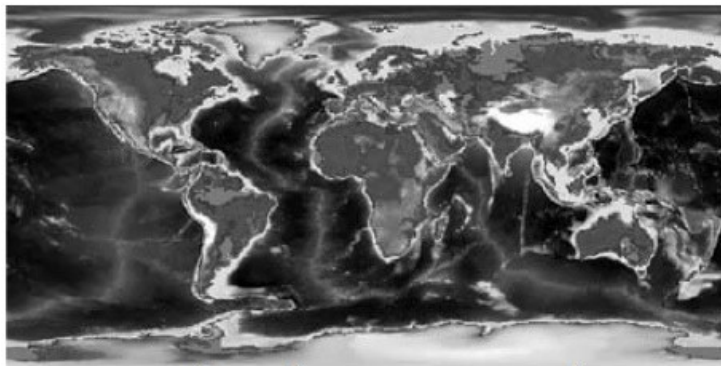
Textures

- There are basically two ways of texture mapping:
 - 2D
 - 3D
- Let us look first at 2D textures
- Image data (surface pixel colors) is stored in a 2D image, the pixels of which are called texels
- Let's assume the coordinates of the image are called u, v and that u and v vary in the interval $[0, 1]$

- To compute what colour is reflected by the sphere, one must find a correspondence between sphere and the texture space
- Parametric sphere:

$$\begin{cases} x = x_c + R \cos\psi \sin\vartheta \\ y = y_c + R \sin\psi \sin\vartheta \\ z = z_c + R \cos\pi \end{cases}$$

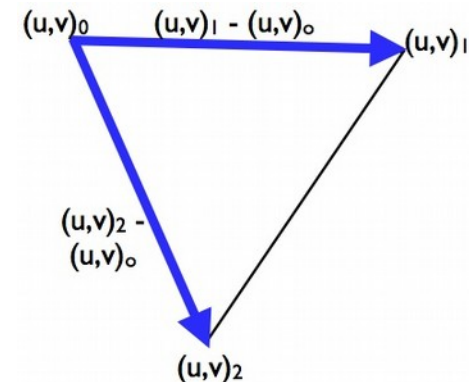
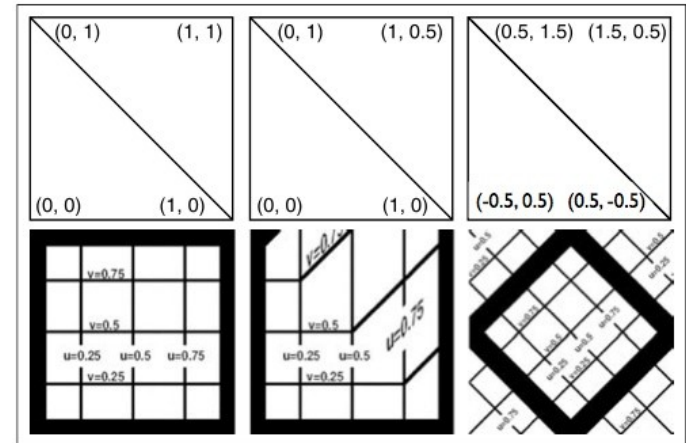
$$\begin{aligned} & \frac{(z - z_c)/R}{\psi = \arctan((y - y_c)/(x - x_c))} \quad \left. \begin{array}{l} \\ \end{array} \right\} \begin{array}{l} \text{longitude} \\ + \text{latitude} \end{array} \\ & \begin{array}{l} u = \psi / 2\pi \\ v = (\pi - \vartheta) / \pi \end{array} \quad \left. \begin{array}{l} \\ \end{array} \right\} \text{to texture} \end{aligned}$$



- Similarly, for other simple maps
 - Cube
 - Cylinder
 - Plane

Textures

- And what if my object is a mesh?
- Determine texture coordinate for each vertex of the mesh
- Bilinear interpolation between vertices
 - For triangles, use barycentric coordinates (same as done for normals)
- If texture coordinates are beyond the image, then



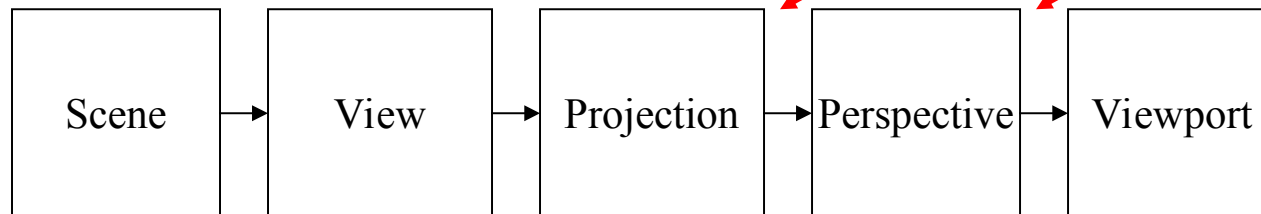
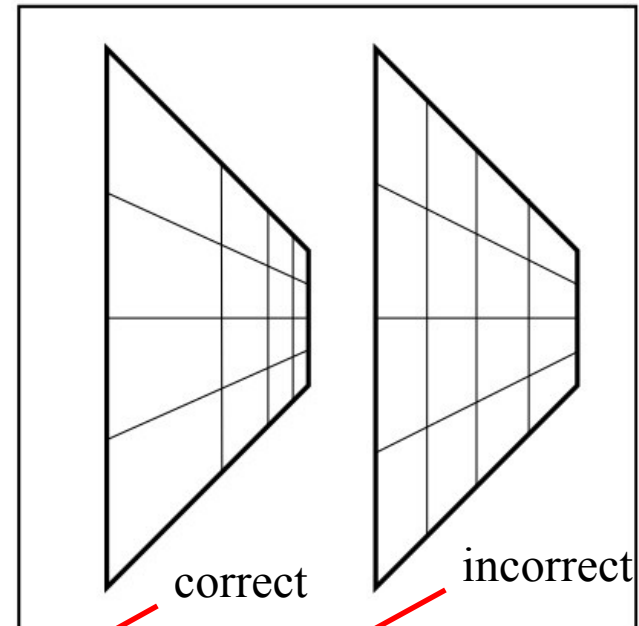
$$u(\beta, \gamma) = u_0 + \beta(u_1 - u_0) + \gamma(u_2 - u_0)$$

$$v(\beta, \gamma) = v_0 + \beta(v_1 - v_0) + \gamma(v_2 - v_0)$$



Correct Textures

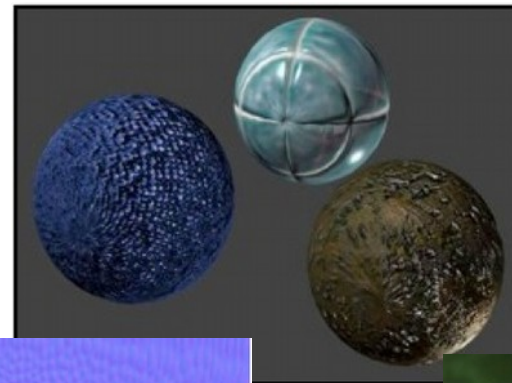
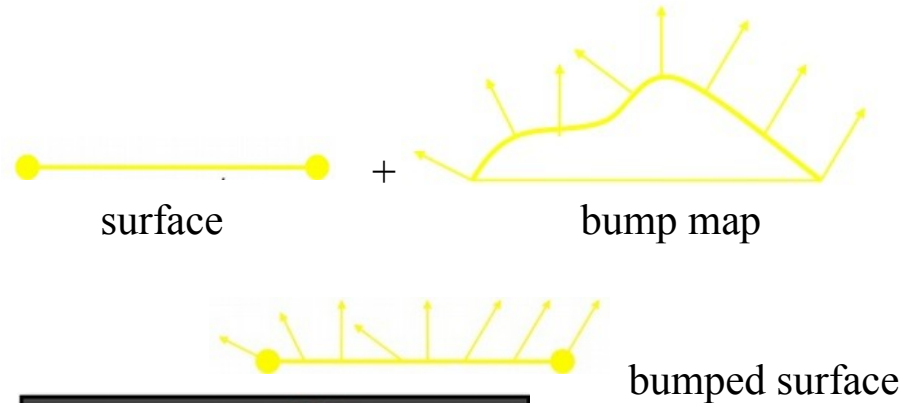
- Be careful when you apply the texture to your object!
 - applying textures in screen space leads to WRONG results!
 - One has to apply the texture BEFORE the perspective is done!
- Otherwise perspective is lost in the texture!
- This is different from what we do in shading, where things are done in screen space



Should we do the math?

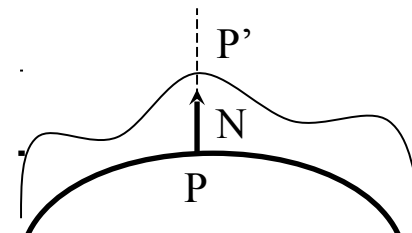
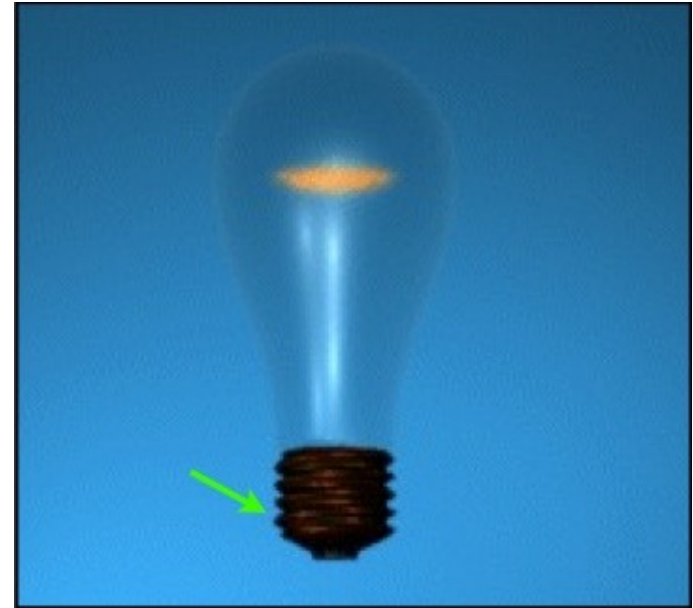
Bump maps

- Textures help with the color of the pixels to be drawn
- However, the resulting objects still look flat
- To improve this, one can store in a texture (bump map) normal variations, and use it for lighting computations while rendering
- This achieves a bumpy surface
- However, when bump mapped polygons are seen from a flat angle they show their flatness



Displacement maps

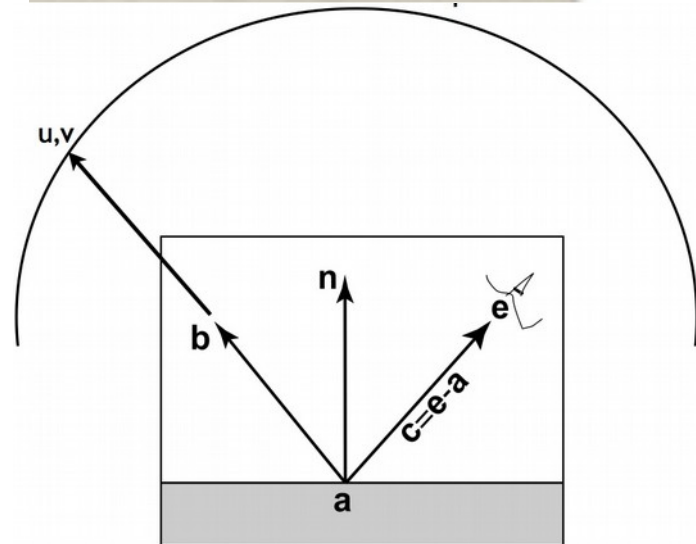
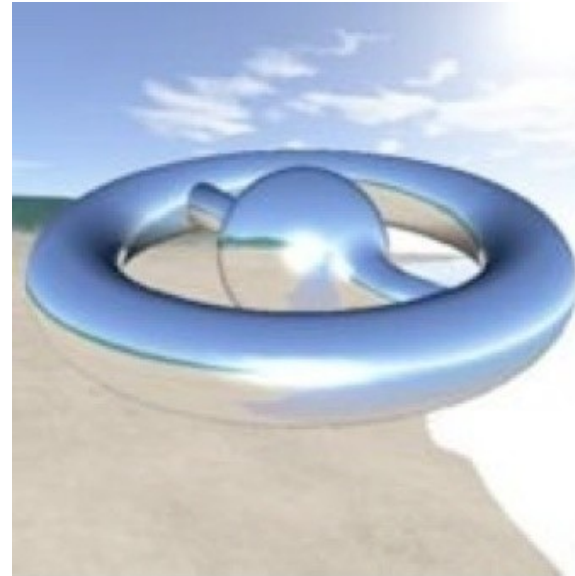
- Bump maps do not modify geometry height, which does not look good from the profile
- A way to correct this is to interpret an additional black and white texture as displacement offsets along the normal
- This is called a displacement map
- Since the displacement map “modifies” the surface to add detail to it, usual lighting computations can be done in the result



Surface + displacement

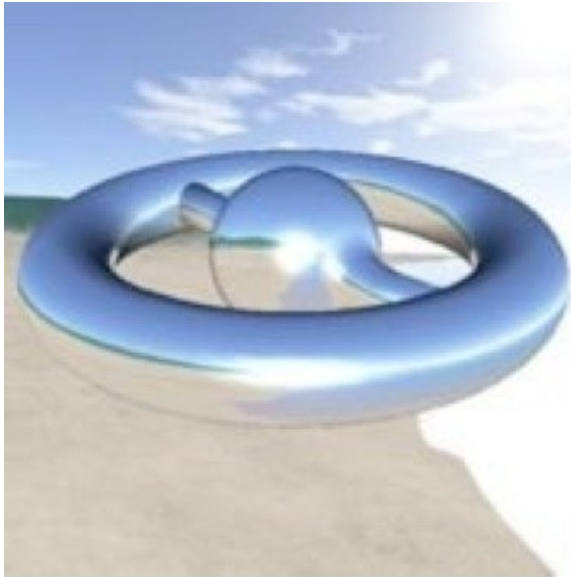
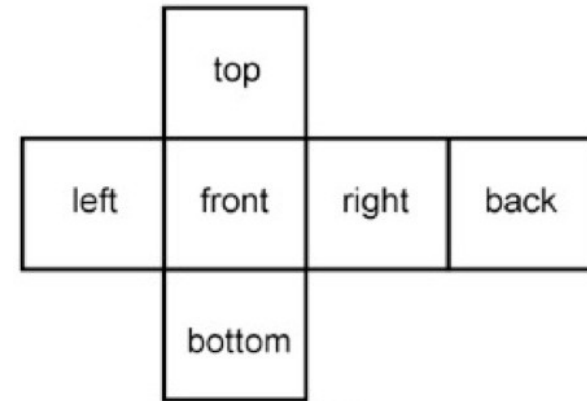
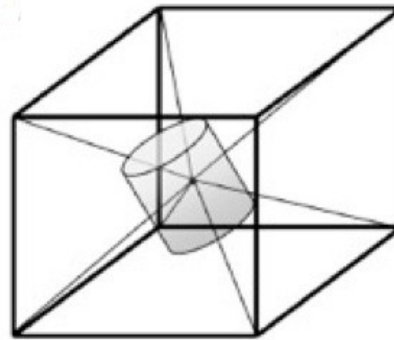
Environment maps

- There are many ways to use textures to obtain special effects in a picture
- Environment maps are used to simulate reflections on objects
- In this case, the world is surrounded by a closed surface having a texture
- The colour at the pixel to be rendered is looked up on the texture according to the reflection ray
-



Environment maps

- There are two different ways of surrounding the world with a surface
- With a sphere: spherical maps
- With a cube: cube maps



Projective texture maps

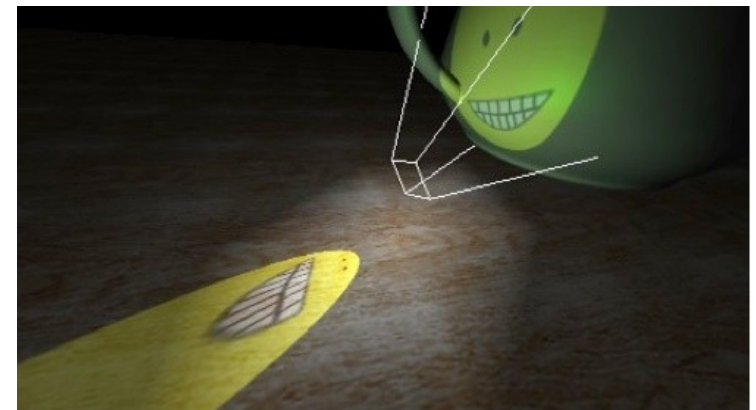
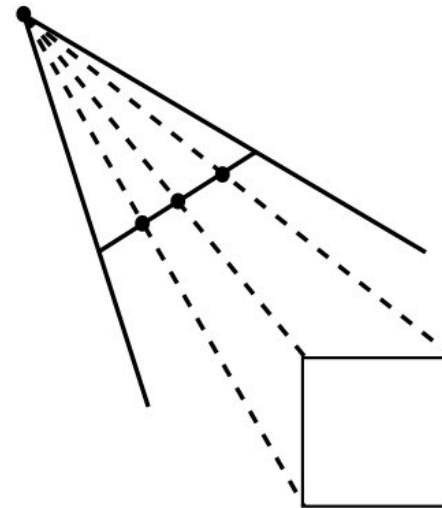
- Projective texture maps work like beamer projection:

- Texture coordinates of a vertex are mapped to texels projected from a given perspective
- What this does is to add a perspective projection from a texture positioned in space
- One needs to find out a mapping M_{d2t} from normalized device coordinates $[-1,1]$ to texture coordinates $[0,1]$.
- M_s =scene transformation
 M_v =view projector transformation
 M_{pp} =persp. projection of projector
 h =homogeneous coords for perspective division

- Then $t = M_{d2t}(M_{pp}M_vM_s v)/h$,

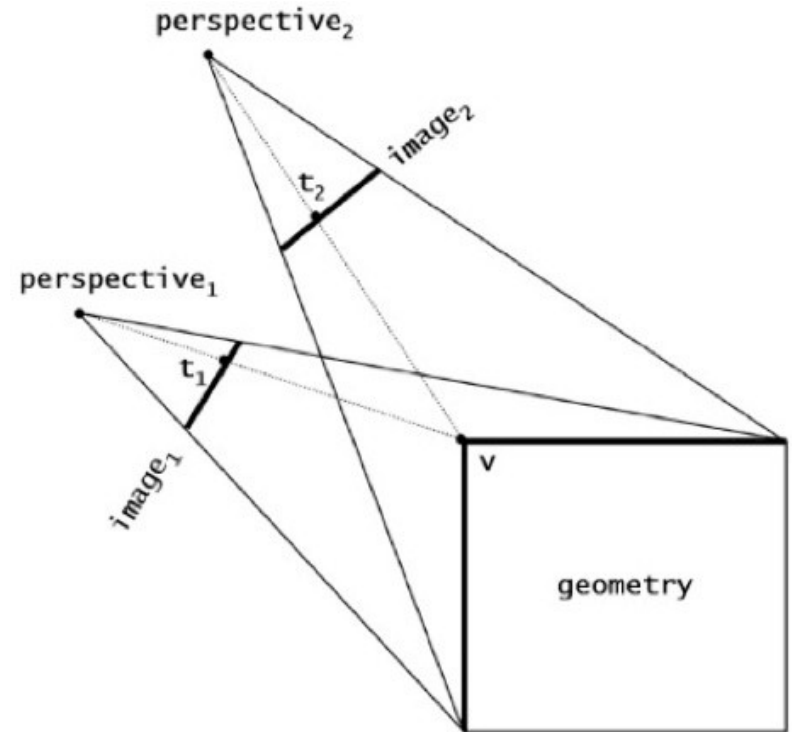
where

$$M_{d2t} = \begin{bmatrix} 0.5 & 0 & 0.5 \\ 0 & 0.5 & 0.5 \\ 0 & 0 & 1 \end{bmatrix}$$



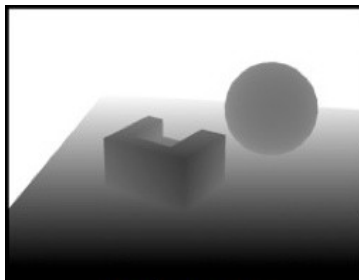
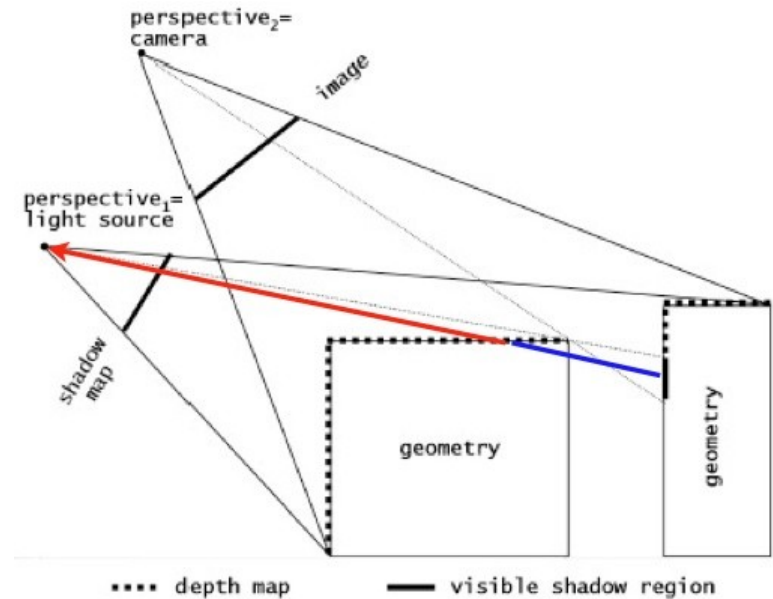
Projective texture maps

- One can use perspective texture maps to warp one perspective into another one:
 - Render image1 from perspective1
 - Compute projective texture coordinates for perspective1 and assign them to the vertices
 - Render scene from perspective2 from texture mapped from image1 and the computed projective textures coordinates
 - For texturing, this is not so interesting, because the result is almost the same as rendered from perspective2
 - However, image1 can be an arbitrary texture

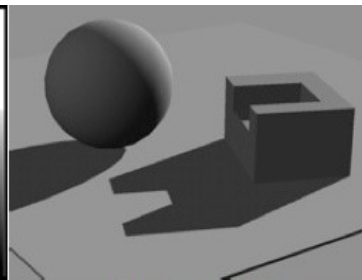


Shadow maps

- One of them can for example contain shadow information to allow hard shadows in my environment
- In this case, you set perspective₁ at the light source, and image₁ contains z-buffer values of the scene from the light source
- When rendering the scene, at each pixel one is rendering one looks if its distance from the light source is smaller or bigger than the z-buffer from the light source
- In case it is bigger, then this point is in the shadow of something else



shadow map
1st pass

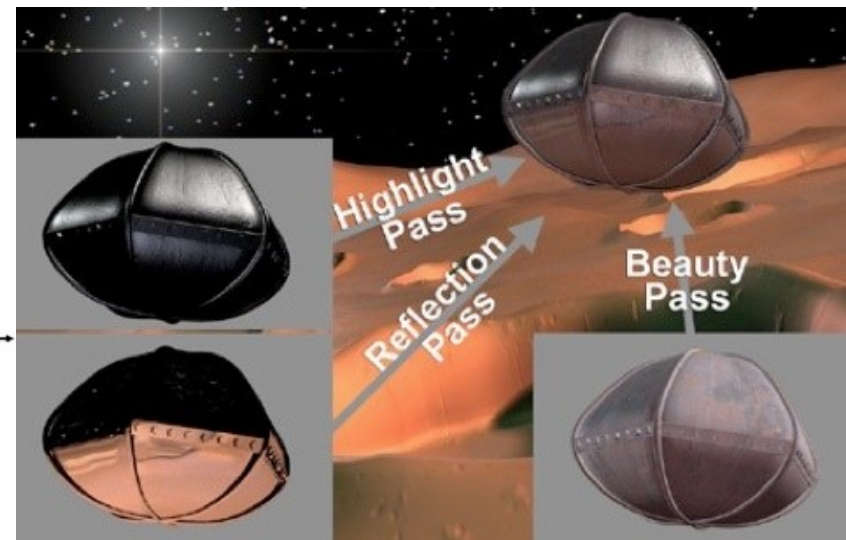
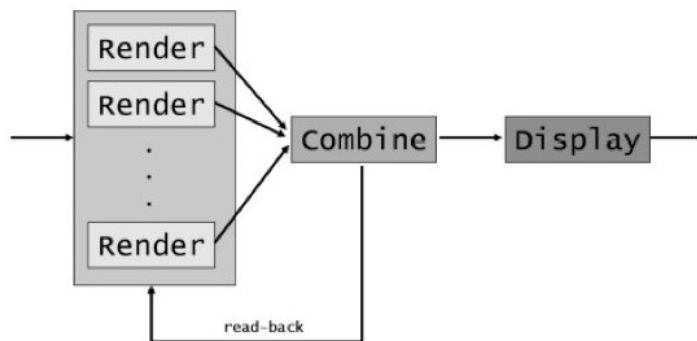


final rendering
2nd pass



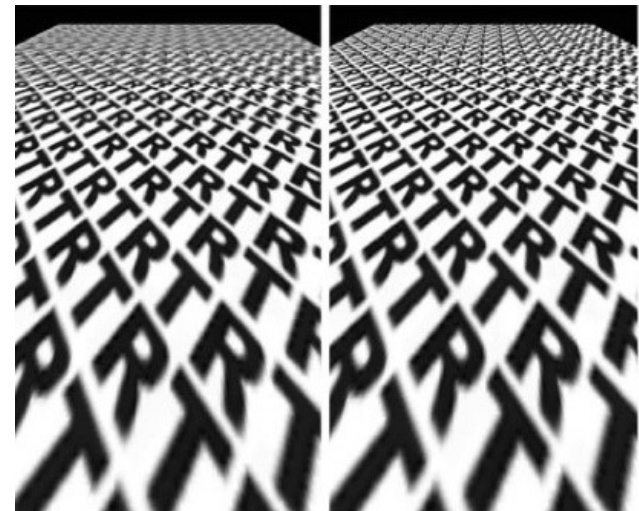
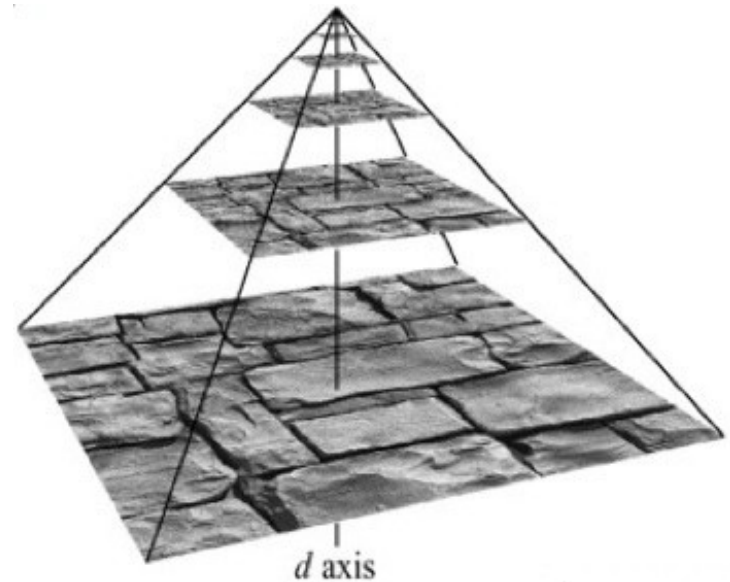
Multi-pass rendering

- To achieve more complex rendering effects, different texture rendering passes are rendered to a texture and not displayed
- This allows the layering of different effects, by blending the results of different rendering passes
- This is called multi-pass rendering



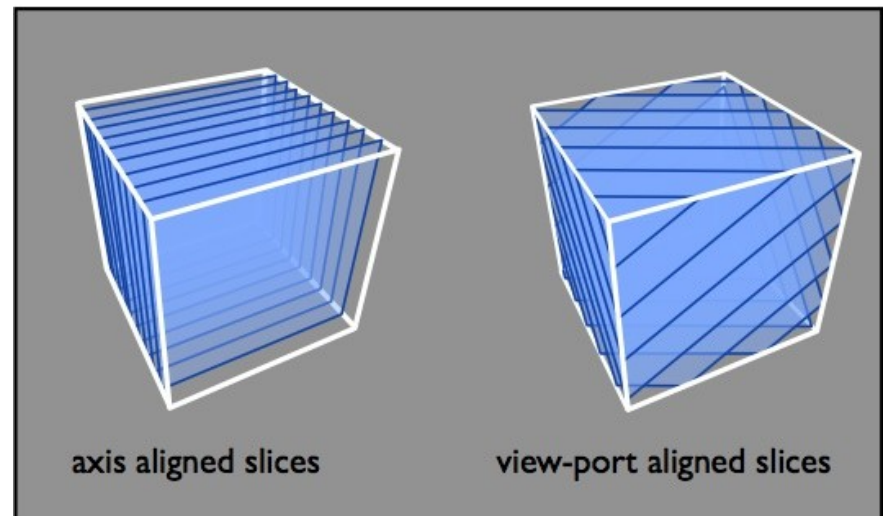
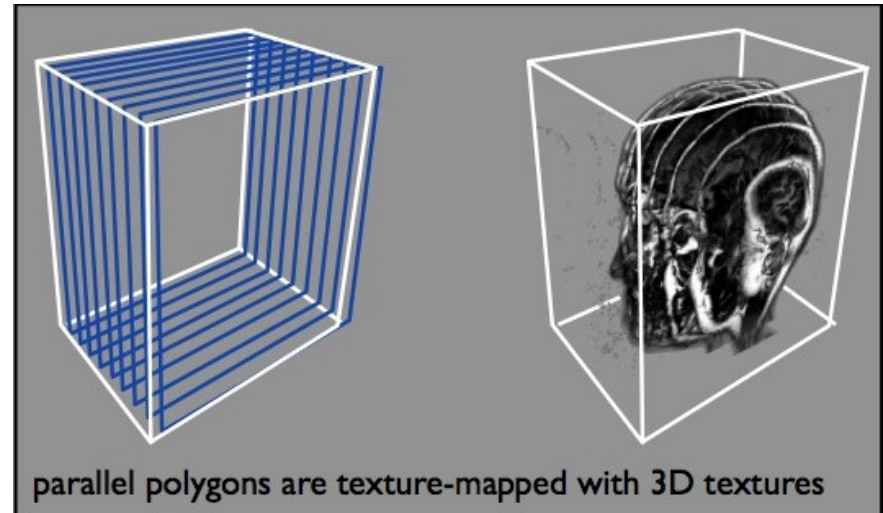
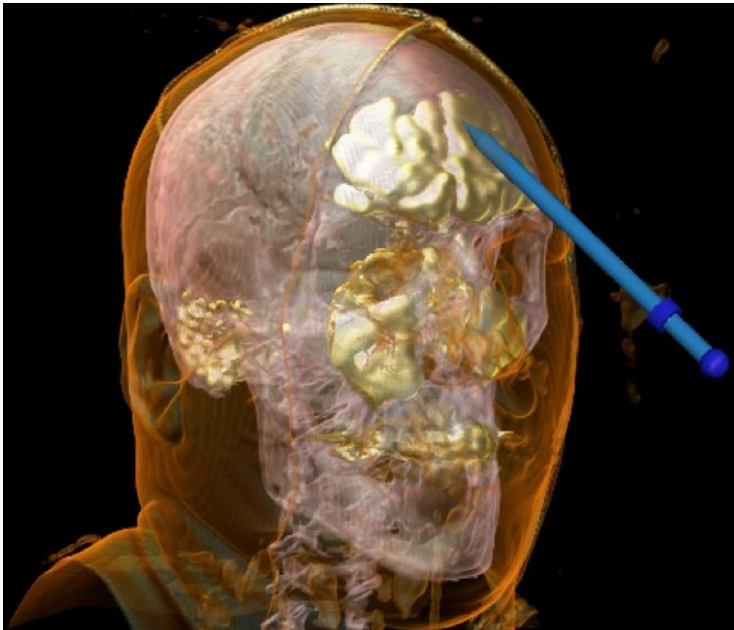
Mip-mapping

- The visual quality of the image depends also from texture resolution with respect to the portion of the screen occupied
- One can define lower resolution textures for scene parts that do not need so much detail
 - This is done by decreasing the resolution of the texture
- Transitions between different levels of detail have to be carefully computed, for example with bilinear interpolation



3D textures

- For volume data, colour can be given by looking up in a 3D texture
- But we will not go into detail with this



End

+++ Ende - The end - Finis - Fin - Fine +++ Ende - The end - Finis - Fin - Fine +++